

AOE 4144: Applied CFD

A series of 12 lectures by Prof. Raj (course co-instructor)

Reflections on the Effectiveness of Applied Computational Aerodynamics for Aircraft Design

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<u>Lecture 4</u>

Topic 4: Emergence of Computational Fluid Dynamics



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At the Dawn of the 20th Century...

17 December 1903 to be precise—the first manned, controlled, powered flight by the Wright brothers!

Orville Wright's telegram to his father:

Success. Four flights Thursday morning. All against twenty one mile wind. Started from level with engine power alone. Average speed through air thirty one miles. Longest 57 seconds. Inform press. Home Christmas.

"This flight lasted only twelve seconds, but it was nevertheless the first in the history of the world in which a machine carrying a man had raised itself by its own power into the air in full flight, had sailed forward without reduction of speed and had finally landed at a point as high as that from which it started.

- Orville Wright

Orville and Wilbur

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Dramatic evolution of civil and military aviation followed

...12 Seconds Changed Human History Forever!



Analytical Fluid Dynamics

Summary Assessment of the State of the Art (early 1900s)

- AFD witnessed notable advances over the preceding 150 years (1750–1900)
 - Development of the governing equations of inviscid (Euler) and viscous flows (Navier-Stokes & RANS)
 - Advances in novel mathematical tools and techniques (such artifacts as sources, sinks, doublets, vortex filaments, etc.) used to obtain <u>analytical solutions</u> of irrotational (potential) and rotational flows of perfect or ideal fluids
- But available AFD capabilities woefully inadequate to meet the emerging needs of airplane engineering design
- AFD offered no satisfactory solution for the problem of resistance—a critical need for airplane design!
 - d'Alembert's paradox (1749-1752) remains unresolved even after 150 years!
 - "In a velocity field that is uniform at infinity and tangent to the body along its surface...
 [body] would suffer no force from the fluid, which is contrary to experience"
 - "Surface of Discontinuity" Theory proposed by Hermann von Helmholtz (1858-1868)
 - "Any geometrically complete sharply-defined edge at which fluids flow past must tear itself from the most typical velocity of the remaining fluid and define a separation surface."
 - Whole resistance being then due to the excess pressure region in front of the body, the dead-water or wake being at approximately the hydrostatic pressure of the fluid.



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Analytical Fluid Dynamics

The Problem of Resistance Challenged Even the Brightest Minds!

On the Resistance of Fluids (Lord Rayleigh F.R.S.)

The London, Edinburgh, and Dublin Philosophical Magazine and Journal of Science, 2:13, 430-441, 1876

(Nearly 125 years after d'Alembert's Paradox was published!)

"There is no part of hydrodynamics more perplexing to the student than which treats the resistance of fluids. According to one school of writers a body exposed to a stream of perfect fluid would experience no resultant force at all, any augmentation of pressure on its face due to the stream being compensated by equal and opposite pressures on its rear...On the other hand it is well known that in practice an obstacle does experience a force tending to carry it downstream and of magnitude too great to be the direct effect of friction; while in many of the treatises calculations of resistance are given leading to results depending on the inertia of the fluid without any reference to friction."

John William Strutt 3rd Baron Rayleigh



Nobel Prize in Physics (1904) 12 Nov 1842 – 30 Jun 1919

Prevailing Wisdom:

Fluid Friction Too Small to Produce Significant Resistance Force!



Finally a Breakthrough in 1904! <u>Prandtl's Boundary Layer Theory</u>

Über Flussigkeitsbeweging bei sehr kleiner Reibung. Verhandlungen Des Dritten Internationalen Mathematiker-Kongresses,

Heidelberg, Vom 8, Bis 13, August 1904, pp 484-491

"The most important aspect of the problem is the behavior of the fluid on the surface of the solid body. The physical processes in the boundary layer [Grenzschicht] between fluid and solid body can be calculated in a sufficiently satisfactory way if *it is assumed* that the fluid adheres to the walls, so that the total velocity is either zero or equal to the velocity of the body. If, however, the viscosity is very small and the path of the fluid along the wall not too long, the velocity will have its normal value very near to the wall. In the thin transition layer (Ubergangsschicht) the sharp changes of velocity, in spite of the viscosity coefficient, small produce noticeable effects."



Ludwig Prandtl



German Physicist 4 Feb 1875 – 15 Aug 1953



Fig. 1.

"A Most Extraordinary Paper of the 20th Century, and Probably of Many Centuries!" — Sydney Goldstein, Harvard Univ.

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Prandtl's Solution of Boundary Layer Equations

Über Flussigkeitsbeweging bei sehr kleiner Reibung.

Verhandlungen Des Dritten Internationalen Mathematiker-Kongresses, Heidelberg, Vom 8, Bis 13, August 1904, pp 484-491

"If, as usual, dp/dx is given throughout, and furthermore the variation of u for the initial cross-section of the flow, then every problem of this kind may be mastered numerically, in that one can obtain from every value of u the corresponding $\partial u/\partial x$ by quadrature. With this and the help of one of the familiar approximate methods, one can repeatedly move a step at a time in the x direction. Of course a difficulty exists with various singularities arising at solid boundaries. The simplest case of the flow situations considered here is the one in which water flows along a thin flat plate. A reduction in the variables is possible here; one can put $u = f\left(\frac{y}{\sqrt{x}}\right)$. One comes up with a formula for the flow resistance using a numerical result of the resulting [ordinary] differential equation

$$R = 1.1 \cdots b \sqrt{k \rho l u_0^3}$$

Ludwig Prandtl



German Physicist 4 Feb 1875 – 15 Aug 1953

(b width, l length of the plate, u_0 the velocity of the undisturbed water opposite the plate)."

• The corresponding skin-friction drag coefficient (for both surfaces of the plate) is

$$C_F = 2.2/\sqrt{Re}$$
 where $Re = \frac{(\rho u_0 l)}{k}$

More accurate calculations later corrected the factor 2.2 to 2.656

A Remarkable Achievement!



Boundary Layer Separation and Vortex Generation

Über Flussigkeitsbeweging bei sehr kleiner Reibung.

Verhandlungen Des Dritten Internationalen Mathematiker-Kongresses, Heidelberg, Vom 8, Bis 13, August 1904, pp 484-491

"<u>The most important result</u> of the investigation <u>for application is</u> that, in certain cases, the flow will separate from the wall at a place completely determined by the external conditions. A fluid layer, which has been set in rotation by the friction at the wall, makes its way into the free fluid where, causing a complete transformation in the motion, it plays the same role as the Helmholtz surface of discontinuity."



Ludwig Prandtl

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German Physicist 4 Feb 1875 – 15 Aug 1953

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"A change in the viscosity coefficient k alters the thickness of the vortex layer (proportional to $\sqrt{kl/\rho u}$) but everything else remains unchanged. Therefore, one can go over to the limit k = 0 and obtain the same flow picture."

Necessary condition for flow separation: pressure increase along the surface in the flow direction

A Singular Contribution of Enormous Lasting Influence for Explaining Otherwise Baffling Fluid Flow Phenomena

Fig. 2.



F. W. Lanchester



British Engineer 23 Oct 1868 - 8 Mar1946

"Numerical work has been done by the aid of an ordinary 25 cm. slide rule, with a liability to error of about 1/5th of 1 percent, an amount which is quite unimportant."

Aerodynamics (early 1900) Became the Most Exciting Research Frontier

AERODYNAMICS

CONSTITUTING THE FIRST VOLUME OF A COMPLETE WORK ON AERIAL FLIGHT

F. W. LANCHESTER

With Appendices on the Velocity and Momentum of Sonnd Waves, on the Theory of Soaring Flight, etc

LONDON ARCHIBALD CONSTABLE & CO. LTD. ORANGE STREET LEICESTER SQUARE



"...the author desires to record his conviction that the time is near when the <u>study of Aerial</u> <u>Flight</u> will take its place as <u>one of the foremost</u> <u>of the applied sciences</u>, one of which the underlying principles furnish some of the most beautiful and fascinating problems in the whole domain of practical dynamics."

"In order that real and consistent progress should be made in Aerodynamics and Aerodonetics, apart from their application in the engineering problem of mechanical flight, it is desirable, if not essential, that provision should be made for the special and systematic study of these subjects in one or more of our great Universities, provision in the form of an adequate endowment with proper scope for its employment under an effective and enlightened administration."

"...<u>the country in which facilities are given for</u> <u>the proper theoretical and experimental study</u> <u>of flight will inevitably find itself in the best</u> <u>position to take the lead in its application and</u> practical development."

The First Half of the 20th Century: Golden Age of Advances in Aerodynamics



Aerodynamics Research Frontiers The First Half of the 20th Century

Analytical Aerodynamics Boasts Pioneering Research

 Rapid increase in fundamental understanding of aerodynamic phenomena provided the much-needed aeronautical knowledge to systematically guide design of aircraft

Experimental Aerodynamics Witnesses Rapid Progress

 Advances stimulated by the urgency of supporting known and anticipated needs of aircraft design that could not be met by analytical aerodynamics due to its inadequacies of simulating realistic flows on complex geometries

Numerical Aerodynamics Exhibits Tremendous Advances

 Aimed at developing methods for applying the differential equations of flow physics in the approximate form of difference equations to overcome the shortcomings of analytical methods

Digital Computers Fuel Neumann's Vision of Solving PDEs

 Use highly efficient digital computers to break the stalemate created by the failure of the purely analytical approach to solve nonlinear partial differential equations (PDEs) such as those governing fluid flows



Analytical Aerodynamics: the 1900s

A Small Sampling of Pioneering Research

 Kutta (1902) – solution of inviscid 2D flow about circular-arc body at zero incidence with circulation and finite velocity at trailing edge Martin Kutta





German Mathematician 3 Nov 1867 – 25 Dec 1944

- **Prandtl-Meyer (1908)** oblique shocks and expansion fans in supersonic flows
- Zhukovskii (1910) design of airfoil sections using graphical construction



- Prandtl (1904) boundary layer theory and vortex generation
- Zhukovskii (1906) circulation theory of lift on 2D airfoils

 $l = \rho \, \Gamma V$

Chaplygin (1910) Postulate: "out of infinite number of theoretically possible solutions past an airfoil with sharp trailing edge, the flow that's nearest to experiment İS the finite one with velocity at the trailing edge"



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Russian Scientist, Mathematician 5 Jan 1847 – 17 Mar 1921

Sergey Chaplygin



Russian Physicist, Mathematician, Engineer 5 Apr 1867 – 8 Oct 1942



Analytical Aerodynamics: the 1910s A Small Sampling of Pioneering Research

- Kármán (1911) first paper on vortex street in the wake of 2D cylinders; referred to Boundary
 Layer theory to explain vortex formation
- Blasius (1912) friction factor in turbulent pipe flows varied as inverse of the 1/4th power of Reynolds number, and velocity as the 1/7th power of the distance from the wall





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 Prandtl (1914) – explained small drag coefficients for spheres with turbulent boundary layer that were first demonstrated by Eiffel in 1912





Prandtl (1918-1919) – classic papers on 3D airfoil (wing) theory of large but finite aspect ratio

$$W = \varrho \int_{a}^{b} \Gamma w \, dx$$
$$w(x) = \frac{1}{4\pi} \int_{a}^{b} \frac{d\Gamma}{dx'} \cdot \frac{dx'}{x - x'}$$

- Munk (1918) the term "induced drag" and the now well-known "Munk's stagger theorem"
- Betz (1919) screw propeller with minimum energy loss



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Source: Wikipedia; Refs. 4.6, 4.10 to 4.13



Analytical Aerodynamics: the 1920s A Small Sampling of Pioneering Research

- Trefftz (1921) estimate induced drag from wake integral in a far downstream "Trefftz plane"
- Kármán (1921) momentum equations of boundary layer, and Kármán-Pohlhausen approximate method of integration $\tau_0 = \mu \left(\frac{\partial u}{\partial u}\right)$

$$\boxed{\frac{\partial}{\partial t}\int_{0}^{b}\varrho u dy + \frac{\partial}{\partial r}\int_{0}^{b}\varrho u^{2} dy - u_{0}\frac{\partial}{\partial x}\int_{0}^{b}\varrho u dy = -\delta\frac{\partial p}{\partial x} - R}$$

Flat plate skin friction formulas for laminar & turbulent boundary layers!

 Taylor (1923) – "Stability of viscous liquid contained between two rotating cylinders"







• **Prandtl (1925)** – "mixing path (or distance) theory" for turbulent flows with the proposition: *momentum is a transferable property*

$$\tau = \varrho l^2 \left| \frac{d u}{d y} \right| \cdot \frac{d u}{d y} \quad \mu_T = \varrho l^2 \left| \frac{d u}{d y} \right| \quad "...a first rough approximation."$$

• Glauert (1928) – Prandtl-Glauert rule for inviscid compressible flows: $C_p = C_{p_0}/\beta$



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Theodore von Kármán



Hungarian-American Mathematician, Physicist, Aerospace Engineer 11 May 1881 – 6 May 1963

 $\beta^2 = 1 - M_{\infty}^2$



Analytical Aerodynamics: the 1930s

A Small Sampling of Pioneering Research

• Kármán (1930) – logarithmic "law of the wall" for planar turbulent flows

$$U_{\max} - U = -\frac{1}{k} \sqrt{\frac{\tau_0}{\rho}} \left(\log \left(1 - \sqrt{\frac{y}{h}} \right) + \sqrt{\frac{y}{h}} \right)$$

- U_{max} is the difference between wall and channel center
 k is a constant independent of dimensions and Reynolds number, appears to have a value 0.38
- **Taylor (1932)** Proposed that *vorticity, not momentum, is the transferable property* in his paper entitled "*The transport of vorticity and heat through fluids in turbulent motion*"
- **Taylor-Maccoll (1933)** Derived and solved an ordinary differential equation (O.D.E.) with one unknown for supersonic flow past a cone
- Taylor (1935) "Statistical theory of turbulence" whole new direction to turbulent flow research!

Predicted Law of Decay of Turbulence behind grids and honeycombs

$$\frac{\mathrm{U}}{u'} = \frac{5x}{\mathrm{A}^2\mathrm{M}} + \mathrm{constant}.$$



G.I. Taylor



British Physicist, Mathematician 7 Mar 1886 – 27 Jun 1975

A = a constant, determined experimentally should be universalfor all square grids; M = mesh length of a square mesh

• Taylor (1935-37) – modified vorticity-transfer theory with application to flow in pipes



If a series of bodies of same thickness distribution but different thickness ratios ($\delta/b \text{ or } \tau$) are placed in streams of different M_{∞} , then the <u>flow patterns are similar</u> as long they all have equal values of K

Lighthill (1947) – hodograph transformation in transonic flows



Analytical Aerodynamics: *Summary Assessment of Capabilities*

Author's Opinion

In spite of phenomenal advances in the first half of the 20th Century, analytical aerodynamics *(circa 1950)* remained inadequate for simulating realistic flows on *complex* geometries—*and remains* so <u>even today</u>!

"...no exact analytical model describing physically interesting flows that depend significantly on Re [Reynolds number] is known." – Garrett Birkhoff, 1981



American Mathematician 19 Jan 1911 – 22 Nov 1996



Value of Analytical Aerodynamics

In spite of severely limited capabilities of simulating realistic flows on complex geometries, analytical aerodynamics offers unique insights that other approaches do not!

"...<u>skillful application of the equations from the dynamics of ideal fluids</u> <u>quite often brings clarity into such phenomena</u> which in themselves are not independent of the viscosity. The vortex equations, in particular, proved themselves very useful. I may be allowed to mention the <u>vortex street</u> by which we are able to reproduce the mechanism of the form resistance with suitable approximation under stated conditions, although such a resistance is precluded in a fluid which is perfectly inviscid...Another striking example is the <u>theory of the</u> <u>induced drag of wings</u>, which likewise shows the extent of applying the vortex equations without overstepping the bounds of the dynamics of ideal fluids."

– Theodore von Kármán, 1931

Analytical Aerodynamics (a subset of AFD) Remains Indispensable for Better Understanding of Complex Flow Phenomena

Experimental Aerodynamics: 1900 – 1950 An Effective Means of Overcoming Inadequacies of AFD

Rapid progress to support development of new airplane designs

• Bigger tunnels; high-speed tunnels; low-turbulence tunnels; special purpose tunnels; ...



shapes: see TR 460, 1935"

"aircraft development work"

"solve the mysteries of flight beyond Mach 1"

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 Techniques and instruments for accurate measurements (e.g., hot-wire anemometry) and visualization (e.g., Schlieren, interferometry)









Source: NASA websites; Refs. 4.27 & 4.28

L4 Genesis of Numerical Aerodynamics: 1910

The Approximate Arithmetical Solution by Finite Differences of Physical Problems involving Differential Equations, with an Application to the Stresses in a Masonry Dam.

By L. F. RICHARDSON, King's College, Cambridge.

Read January 13, 1910

IX. The Approximate Arithmetical Solution by Finite Differences of Physical Problems involving Differential Equations, with an Application to the Stresses in a Masonry Dam.

By L. F. RICHARDSON, King's College, Cambridge.

Communicated by Dr. R. T. GLAZEBROOK, F.R.S.

Received (in revised form) November 2, 1909,-Read January 13, 1910.

§ 1. INTRODUCTION.—§ 1.0. The object of this paper is to develop methods whereby the differential equations of physics may be applied more freely than hitherto in the approximate form of difference equations to problems concerning irregular bodies.

Though very different in method, it is in purpose a continuation of a former paper by the author, on a "Freehand Graphic Way of Determining Stream Lines and Equipotentials" ('Phil. Mag.,' February, 1908; also 'Proc. Physical Soc.,' London, vol. xxi.). And all that was there said, as to the need for new methods, may be taken to apply here also. In brief, analytical methods are the foundation of the whole subject, and in practice they are the most accurate when they will work, but in the integration of partial equations, with reference to irregular-shaped boundaries, their field of application is very limited.

Both for engineering and for many of the less exact sciences, such as biology, there is a demand for rapid methods, easy to be understood and applicable to unusual equations and irregular bodies. If they can be accurate, so much the better; but 1 per cent. would suffice for many purposes. It is hoped that the methods put forward in this paper will help to supply this demand.

The equations considered in any detail are only a few of the commoner ones occurring in physical mathematics, namely:--LAPLACE's equation $\nabla^2 \phi = 0$; the oscillation equations $(\nabla^2 + k^2) \phi = 0$ and $(\nabla^4 - k^2) \phi = 0$; and the equation $\nabla^4 \phi = 0$. But the methods employed are not limited to these equations.

The Number of Independent Variables.—In the examples treated in the paper this never exceeds two. The extension to three variables is, however, perfectly obvious. One has only to let the third variable be represented by the number of the page of a book of tracing paper. The operators are extended quite simply, and the same VOL COX.—A 467. 2 R 2 24.5.10

Lewis Fry Richardson



FRS, British Mathematician, Physicist, Meteorologist, Psychologist

11 Oct 1881 – 30 Sep 1953



Richardson's Observations: 1910 Paper

"The object of this paper is to develop methods whereby the differential equations of physics may be applied more freely than hitherto in the approximate form of difference equations to problems concerning irregular bodies."

"...analytical methods are the foundation of the whole subject, and in practice they are the most accurate when they will work, but in the integration of partial equations, with reference to irregular-shaped boundaries, their field of application is very limited."

"So far I have paid piece rates for the $\delta_x^2 + \delta_y^2$ operation of about n/18 pence per coordinate point, n being the number of digits. The chief trouble to the computers has been the intermixture of plus and minus signs. As to the rate of working, one of the quickest boys averaged 2,000 operations $\delta_x^2 + \delta_y^2$ per week, for numbers of three digits, those done wrong being discounted."

Extension to Fluid Flows

TO SIMULATE FLOW ABOUT IRREGULARLY SHAPED BODIES

- 1. Use difference form of differential equations of *fluid flow* physics. What
- 2. Cannot apply analytical methods to irregularly shaped bodies.
- 3. Employ 'computers' [humans] to perform arithmetic operations.

The What, the Why and the How of <u>CFD</u> (the rest is DETAIL!)

Why

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Numerical Aerodynamics: 1910 – 1950

- Pioneering Foundational Research in Numerical Methods Parallels Exciting Research in Analytical Aerodynamics
 - **Richardson (1910)** point iterative scheme for Laplace's equation
 - Liebmann (1918) improved version of Richardson's method with faster convergence
 - Courant, Friedrichs, and Lewy (1928) uniqueness and existence of numerical solutions of PDEs (origins of the CFL condition well known to all "CFDers")
 - Southwell (1940) improved relaxation scheme tailored for hand calculations
 - Frankel (1950) first version of successive over-relaxation scheme for Laplace's equation
 - O'Brien, Hyman, and Kaplan (1950) von Neumann method for evaluating stability of numerical methods for time-marching problems

Early Adopters

KEVIN T. CROFTON DEPARTMENT OF AEROSPACE AND OCEAN ENGINEERING

• **Thom (1929-1933)** – flow past circular cylinders at low speeds by numerically solving steady viscous flow equations: *stream function–vorticity* (ψ – ζ) *formulation of the N-S equations*

• Kawaguti (1953) – flow past circular cylinder at Re = 40

- 232 mesh points for half flow region
- Iterative procedure is considered converged when difference between successive approximations for *ψ* and *ζ* does not exceed 0.3% of maximum value for the last 4 cycles
- "The numerical integration in this study took <u>about one</u> <u>year and a half with twenty working hours every week</u>, with a considerable amount of labor and endurance."



The Bottleneck: Slow & Laborious Computing



A Vision for the Future (1946)

"... really efficient high-speed [digital] computing devices may, in the field of non-linear partial differential equations as well as in many other fields...provide us with those heuristic hints which are needed in all parts of mathematics for genuine progress."

"Our present analytical methods seem unsuitable for the solution of the important problems arising in connection with non-linear partial differential equations...The truth of this statement is particularly striking in the field of fluid dynamics."

"The advance of analysis is, at this moment, stagnant along the entire front of non-linear problems...Although the main mathematical difficulties have been known since the time of Riemann and of Reynolds, and although as brilliant a mathematical physicists as Rayleigh has spent a major part of his life's effort in combating them, yet no decisive progress has been made against them—indeed hardly any progress which could be rated as important..." John von Neumann



Hungarian-American Mathematician, Physicist, Computer Scientist 28 Dec 1903 – 8 Feb 1957 <u>1999 Financial Times</u> <u>Person of the Century</u>

"...many branches of both pure and applied mathematics are in **great need of computing instruments to break the present stalemate** created by the failure of the purely analytical approach to nonlinear problems."

These are excerpts from the first paper in Ref. 4.35 entitled "ON THE PRINCIPLES OF LARGE SCALE COMPUTING MACHINES. This paper was never published. It contains material given by von Neumann in a number of lectures, in particular one at a meeting on <u>May 5, 1946</u>, of the Mathematical Computing Advisory Panel, Office of Research and Inventions, Navy Department, Washington, D.C. The manuscript from which this paper was taken also contained material (not published here) which was published in the Report, "Planning and Coding of Problems for an Electronic Computing Instrument".

22 Note: Highlighting by the author.



Digital Computers: 1930 – 1950

- Alan Turing (1936) a universal machine capable of computing anything that is computable
- Atanasoff (1937) first computer without gears, cams, belts and shafts
- Atanasoff and Berry (1941) a computer that can solve 29 equations simultaneously, and store information on its main memory
- Mauchly and Eckert (1943-44) Electronic Numerical Integrator and Calculator (ENIAC) using 18,000 vacuum tubes
 - ✓ Speed: 500 floating point operations per second
 - ✓ Size: 1,800 square feet
- Mauchly and Presper (1946) Universal Automatic Computer (UNIVAC), the first commercial computer for business and government





The Key to Converting von Neumann's Vision into Reality!



Lecture 4: Overarching Takeaways

By 1950, all fundamental ingredients were in place for the evolution of an exciting new field of [what we call] Computational Fluid Dynamics (CFD).

In the second half of the 20th century, phenomenal advances in CFD methods and computing capabilities fueled the evolution of Applied Computational Aerodynamics (ACA).

ACA Evolution was Driven by the Promise of CFD Serving as a Powerful "Alternative" to AFD and EFD for Simulating Aerodynamics of Irregularly Shaped Bodies!



Lecture 4: Key Takeaways

- 1903: the first manned, controlled, powered flight by the Wright brothers!
- Even after 150 years of noteworthy progress, Analytical Fluid Dynamics woefully inadequate to meet the emerging airplane design needs
 - No solution of the problem of resistance in sight. *d'Alembert's paradox rules!*
- 1904: A breakthrough—Prandtl's Boundary Layer theory!
 - "A most extraordinary paper of the 20th century, and probably of many centuries!"
- The first 50 years of the 20th century (1900-1950) witnessed phenomenal advances in Analytical Aerodynamics, but...analytical models remained inadequate for simulating realistic flows on irregularly shaped bodies
 - EFD provided the best means of solving practical engineering problem
- 1910: Richardson laid the foundation of Numerical Fluid Dynamics
 - Use difference form of differential equations; employ human computers to perform resulting arithmetic operations; applicable to irregularly shaped bodies, but...
 - Human computers were the bottleneck!
- 1930 1950: Digital computers evolved
 - Key to realizing von Neumann's 1946 vision: "really efficient high-speed [digital] computing devices may break the present stalemate created by the failure of the purely analytical approach to nonlinear problems"

By 1950, all basic ingredients were in place for the evolution of Computational Fluid Dynamics (CFD)



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